

This is a Fine Mesh You've Gotten Me Into!

John Burkardt

.....

16 November 2021, 11am, 427 Thackeray,
Undergraduate Math Seminar, Jeff Wheeler, moderator.

.....

University of Pittsburgh Mathematics Department

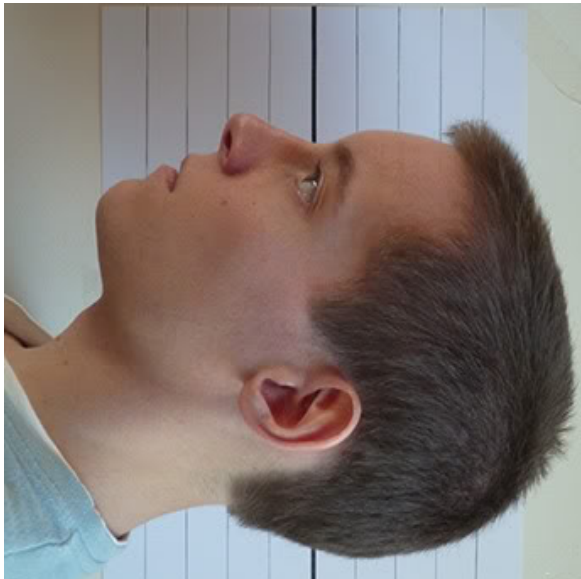
.....

[https://people.sc.fsu.edu/~jburkardt/presentations/...](https://people.sc.fsu.edu/~jburkardt/presentations/... mesh_2021_pitt.pdf)
... mesh_2021_pitt.pdf

2: A Profile (Not Mine!)



3: A Profile Rotated



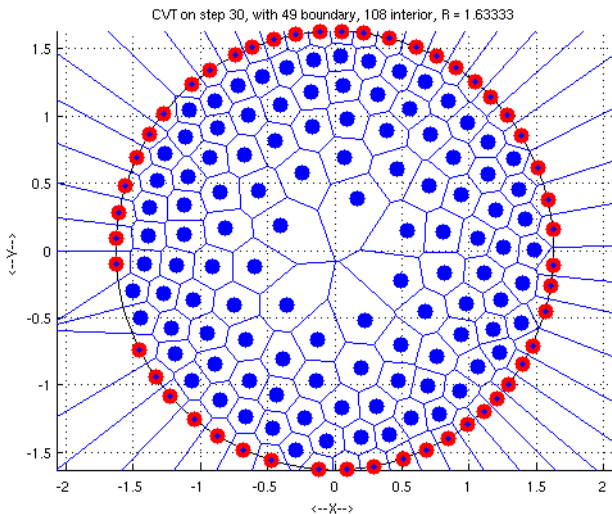
4: A Profile Rotated and Outlined



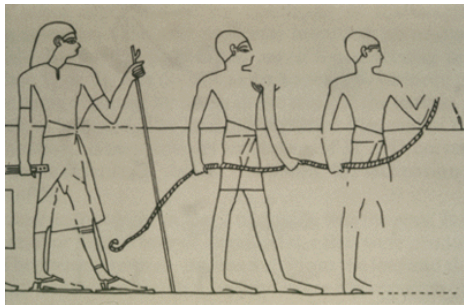
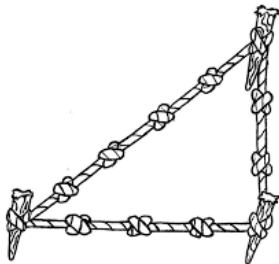
5: A Profile Rotated and Outlined and Extracted



6: A Flower Grown In a Computer?



7: Meshes Started with Taxation

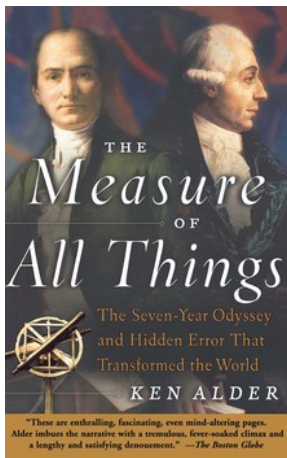
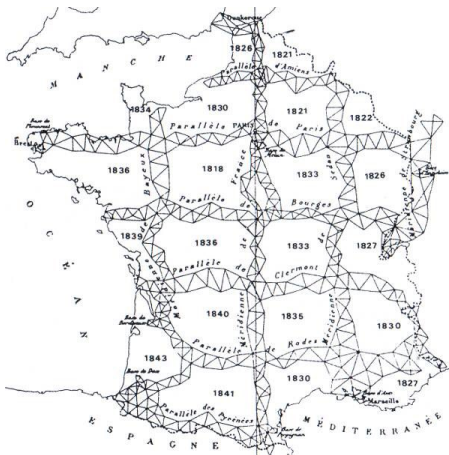


8: A Mesh Organizes and Simplifies a Complicated View



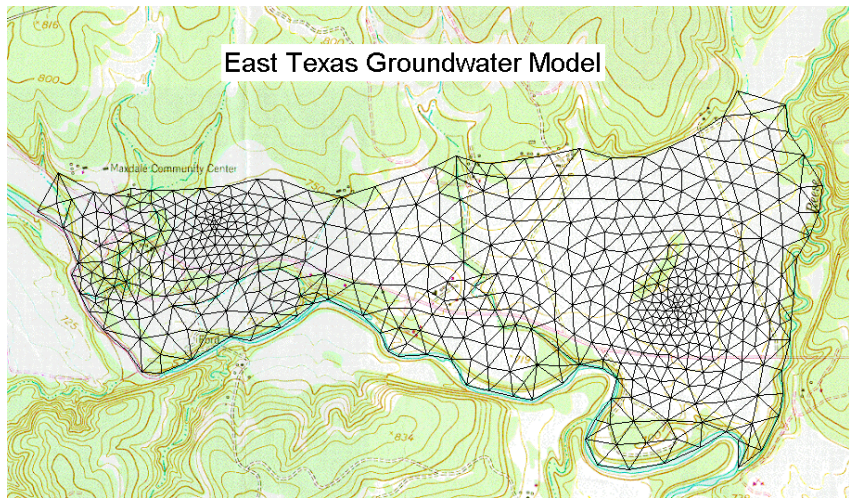
<https://www.metmuseum.org/art/collection/search/366555>

9: A Mesh Can Organize and Measure Curved Surfaces



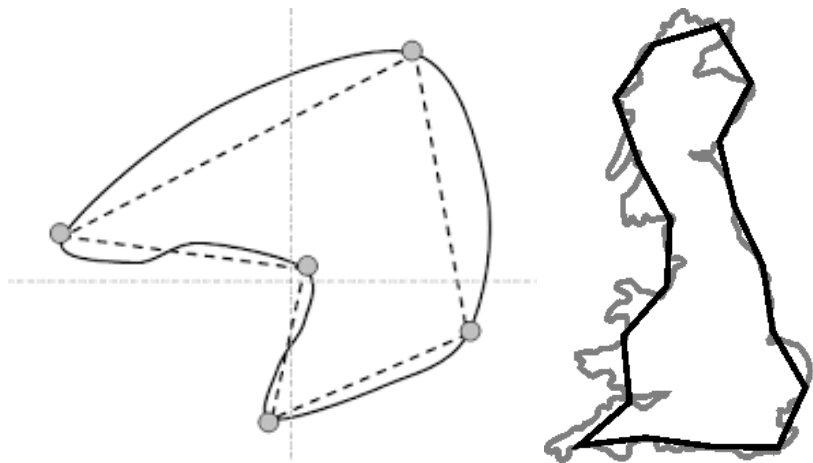
<https://www.simonandschuster.com/books/The-Measure-of-All-Things/Ken-Alder/9780743216760>

10: Computers Model Reality with Meshes

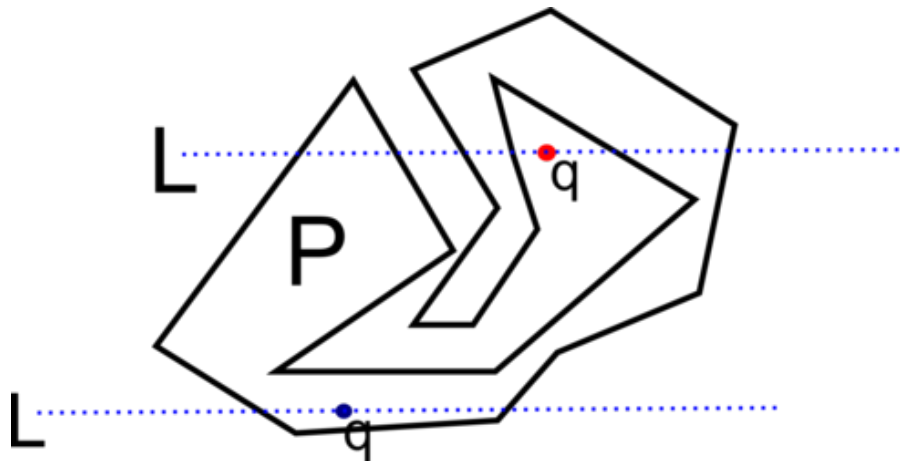


<https://www.cae.utexas.edu/prof/maidment/gishyd97/gms/gms.htm>

11: Computers Approximate Shapes with Polygons



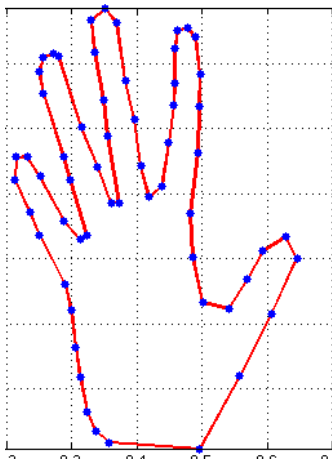
12: Arithmetic is Easy, Geometry is Hard!



13: We Can Automate the Measurements

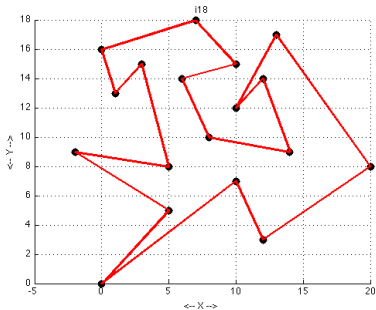
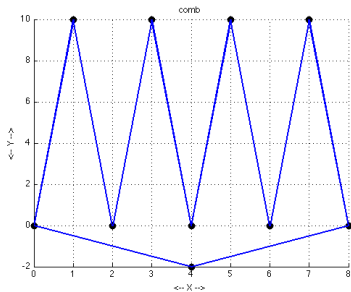
```
% Get the screensize .
%
    screen = get ( 0, 'ScreenSize' );
%
% Use the whole screen as a figure .
%
figure ( 'Position' , screen );
%
% Create a graphical coordinate system on the figure .
%
axes ( 'Position' , [ 0, 0, 1, 1 ] );
%
% The user clicks sample points on the boundary , termin
%
[ x, y ] = ginput ( );
```

14: From Points We Have an outline



https://people.sc.fsu.edu/~jburkardt/m_src/hand_data/hand_data.png

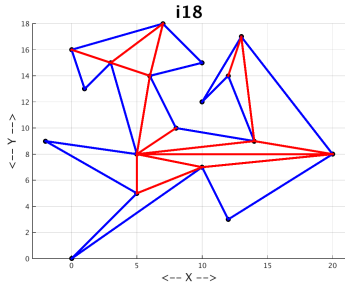
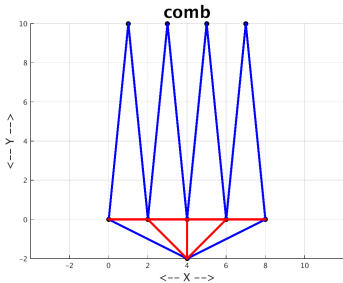
15: Polygons Are a Little Messy



https://people.sc.fsu.edu/~jburkardt/m_src/polygon_triangulate_test/comb.png

https://people.sc.fsu.edu/~jburkardt/m_src/polygon_triangulate_test/i18.png

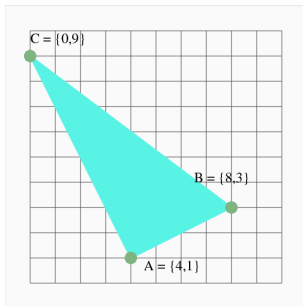
16: But Polygons Can Be Triangulated



https://people.sc.fsu.edu/~jburkardt/m_src/polygon_triangulate_test/comb_triangulation.png

https://people.sc.fsu.edu/~jburkardt/m_src/polygon_triangulate_test/i18_triangulation.png

17: The Area of a Triangle



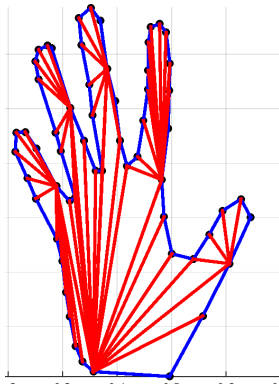
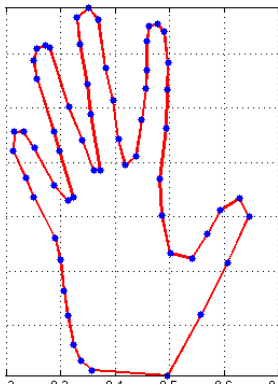
$$\begin{aligned}\text{area}(A, B, C) &= 1/2 \begin{vmatrix} B_x - A_x & B_y - A_y \\ C_x - A_x & C_y - A_y \end{vmatrix} \\ &= 1/2((B_x - A_x)(C_y - A_y) - (B_y - A_y)(C_x - A_x)) \\ &= 1/2((8 - 4)(9 - 1) - (3 - 1)(0 - 4)) \\ &= 20\end{aligned}$$

18: Code for Triangle Area

```
function area = triangle_area ( ax, ay, bx, by, cx, cy )  
  
    area = 0.5 * ...  
        ( ( bx - ax ) * ( cy - ay ) ...  
          - ( cx - ax ) * ( by - ay ) );  
  
    return  
end
```

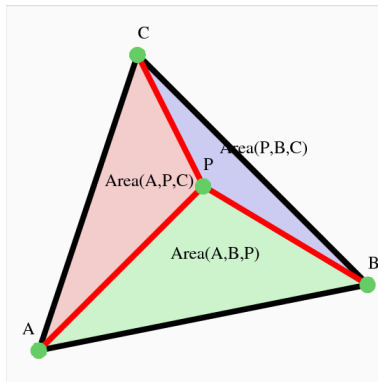
https://people.sc.fsu.edu/~jburkardt/m_src/triangle_properties/triangle_area.m

19: I Can Compute The Area of My (Flat) Hand



https://people.sc.fsu.edu/~jburkardt/m_src/polygon_triangulate_test/hand_triangulation.png

20: Does a Triangle Contain a Point?

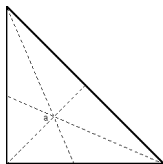


P is inside T if all three areas are positive:

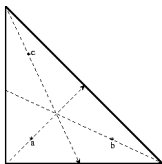
- Area(P,B,C)
- Area(A,P,C)
- Area(A,B,P)

21: Can We Integrate Over a Triangle?

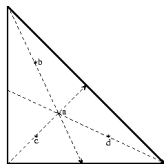
$$\int_T f(x, y) dx dy \approx \sum_{i=1}^n w_k f(x_i, y_i)$$



(a) Linear
 $a = (\frac{1}{3}, \frac{1}{3}), w = 1$

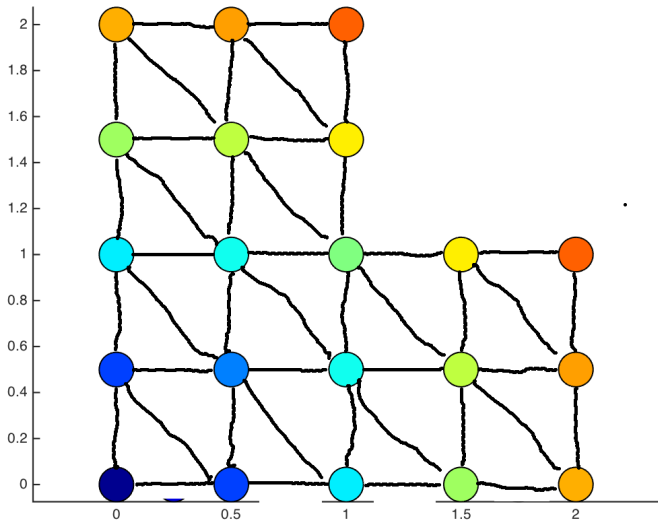


(b) Quadratic
 $a = (\frac{1}{6}, \frac{1}{6}), w = \frac{1}{3}$
 $b = (\frac{2}{3}, \frac{1}{6}), w = \frac{1}{3}$
 $c = (\frac{1}{6}, \frac{2}{3}), w = \frac{1}{3}$

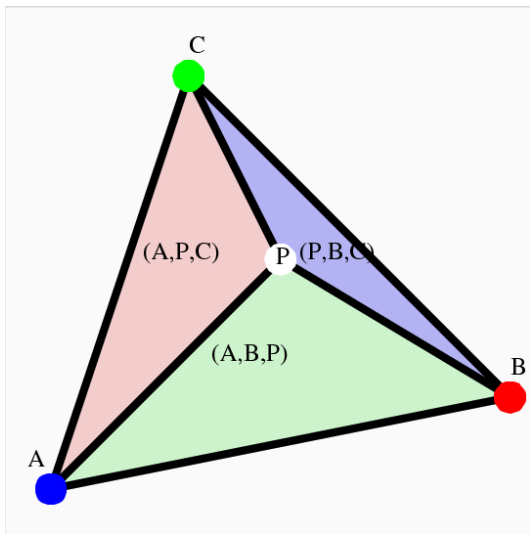


(c) Cubic
 $a = (\frac{1}{3}, \frac{1}{3}), w = -\frac{27}{48}$
 $b = (\frac{1}{5}, \frac{3}{5}), w = \frac{25}{48}$
 $c = (\frac{1}{5}, \frac{1}{5}), w = \frac{25}{48}$
 $d = (\frac{3}{5}, \frac{1}{5}), w = \frac{25}{48}$

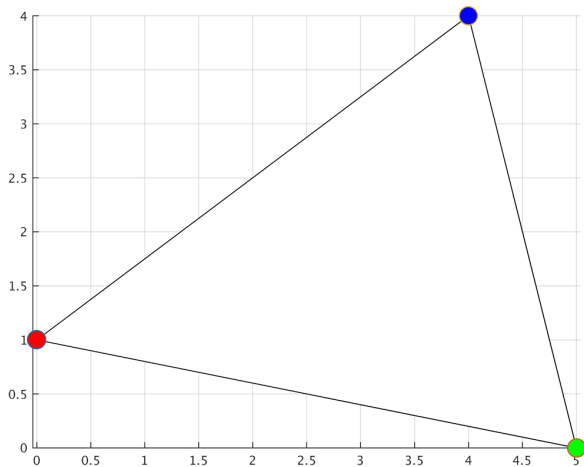
22: Computer Data Only Computed at a Few Points



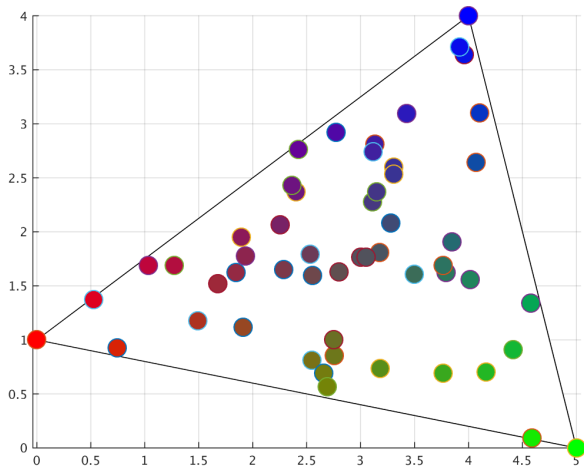
23: Area-Averaging Vertex Values



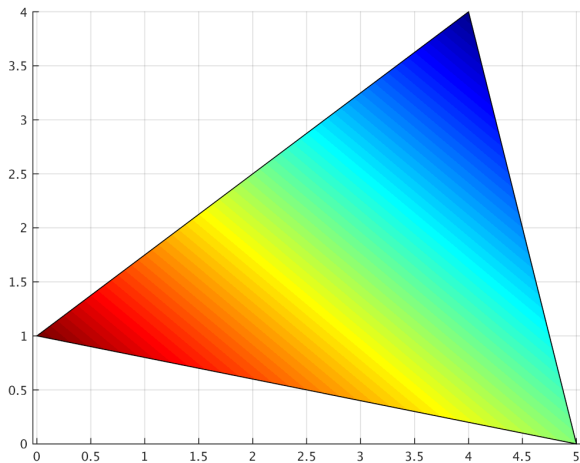
24: We Know the Values at Triangle Vertices



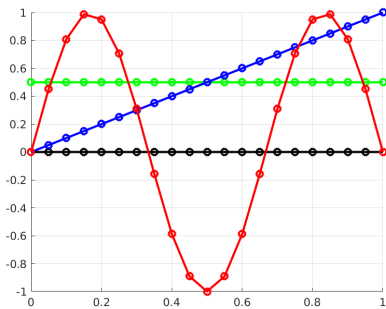
25: Fill Some Points in the Triangle



26: Fill All Points in a Triangle



26.5: Physics is about the bends!



$$\frac{\partial T}{\partial t} = \nabla^2 T$$

$$\nabla T = \frac{\partial T}{\partial x} \approx \frac{T(x + dx) - T(x)}{dx}$$

$$\nabla^2 T = \frac{\partial^2 T}{\partial x^2} \approx \frac{T(x + dx) - 2T(x) + T(x - dx)}{dx^2}$$

27: MESH2D Can Create Internal Nodes

```
[ p, t ] = mesh2d ( v );
```

- v , a list of boundary (x,y) coordinates;
- p , the coordinates of nodes;
- t , triples of nodes forming triangles.

<https://www.mathworks.com/matlabcentral/fileexchange/25555-mesh2d-automatic-mesh-generation>

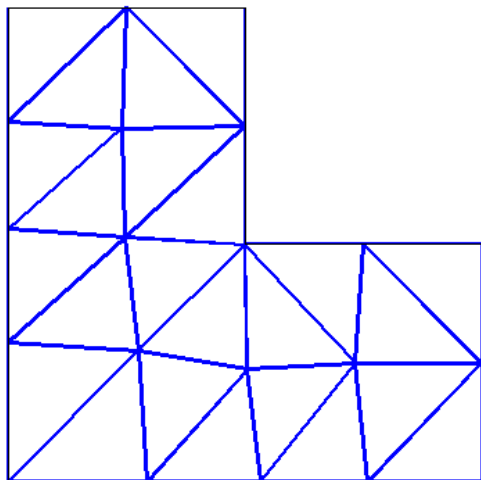
28: MESH2D: Simple ELL Mesh

```
v = [ 0.0, 0.0; ...  
      2.0, 0.0; ...  
      2.0, 1.0; ...  
      1.0, 1.0; ...  
      1.0, 2.0; ...  
      0.0, 2.0 ];
```

```
[ p, t ] = mesh2d ( v );
```

https://people.sc.fsu.edu/~jburkardt/m_src/mesh2d_test/ell_test.m

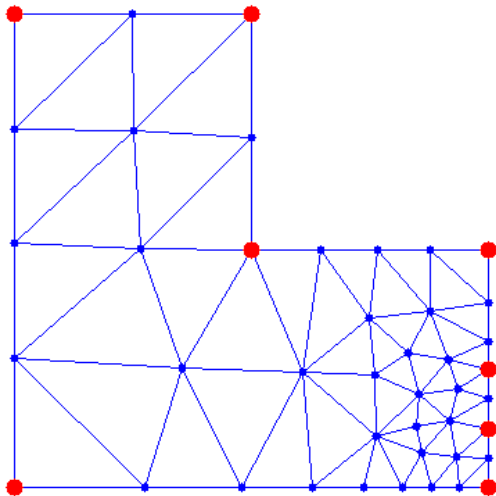
29: MESH2D: Simple ELL Mesh



30: MESH2D: Add Two Short Boundary Segments

```
v = [ 0.0, 0.0; ...  
      2.0, 0.0; ...  
      2.0, 0.25;  
      2.0, 0.5; ...  
      2.0, 1.0; ...  
      1.0, 1.0; ...  
      1.0, 2.0; ...  
      0.0, 2.0 ];  
  
[ p, t ] = mesh2d ( v );
```

31: MESH2D: Two Short Boundary Segments



32: MESH2D: Set Maximum Element Size

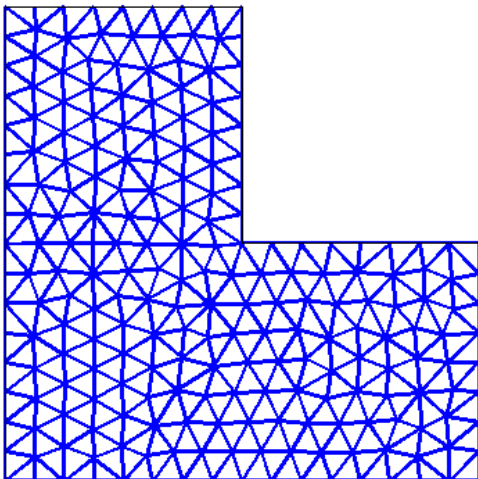
```
v = [ 0.0, 0.0; ...  
      2.0, 0.0; ...  
      2.0, 1.0; ...  
      1.0, 1.0; ...  
      1.0, 2.0; ...  
      0.0, 2.0 ];
```

```
hdata = [];
```

```
hdata.hmax = 0.1;
```

```
[ p, t ] = mesh2d ( v, [], hdata );
```

33: MESH2D: Set Maximum Element Size



34: MESH2D: Use a Density Function

```
v = [ 0.0, 0.0; ...  
      2.0, 0.0; ...  
      2.0, 1.0; ...  
      1.0, 1.0; ...  
      1.0, 2.0; ...  
      0.0, 2.0 ];
```

```
hdata = [];  
hdata.fun = @hfun;
```

```
[ p, t ] = mesh2d ( v, [], hdata );
```

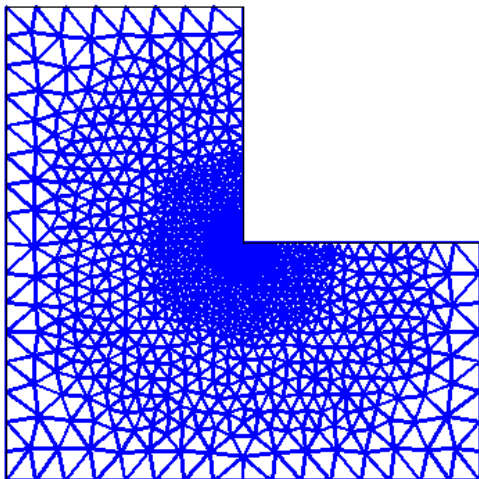
35: MESH2D: A Density Function Controls Mesh Size H

```
function h = hfun ( x, y )

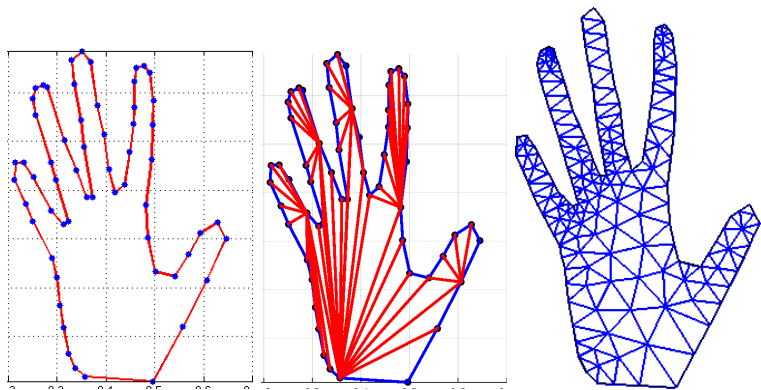
%
% Minimum size is 0.01, increasing as we move away
% from ( 1.0, 1.0 ).
%
  h = 0.01 + 0.1 * sqrt ( ( x-1.0 ).^2 + ( y-1.0 ).^2 );

  return
end
```

36: MESH2D: Ask for a Small Mesh Near the Indentation

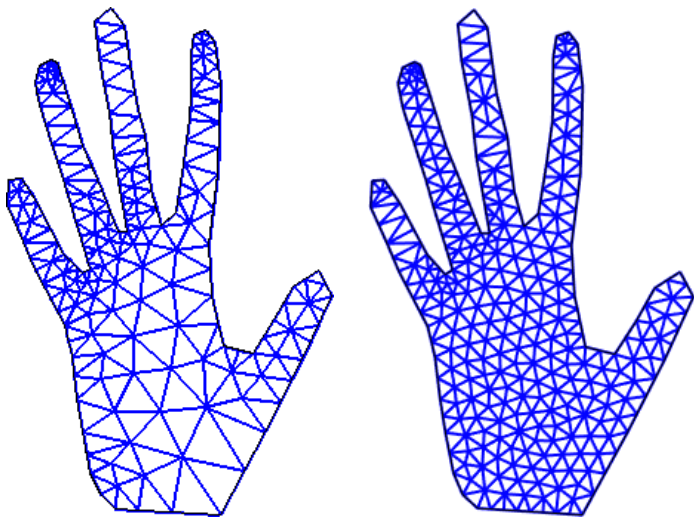


37: Apply MESH2D to the Hand Data

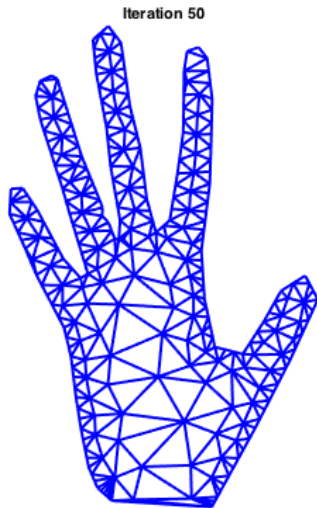


https://people.sc.fsu.edu/~jburkardt/m_src/hand_mesh2d_test/hand_mesh2d_mesh.png

38: Apply MESH2D to the Hand Data



39: A Mesh That's Finest Near the Edge



https://people.sc.fsu.edu/~jburkardt/m_src/distmesh_test/p24_mesh.png

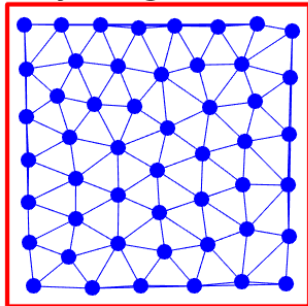
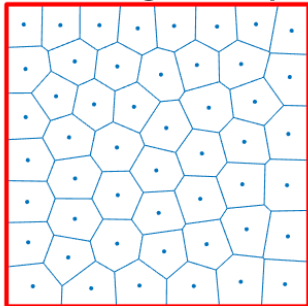
40: A Mesh from Nature



https://en.wikipedia.org/wiki/Centroidal_Voronoi_tessellation

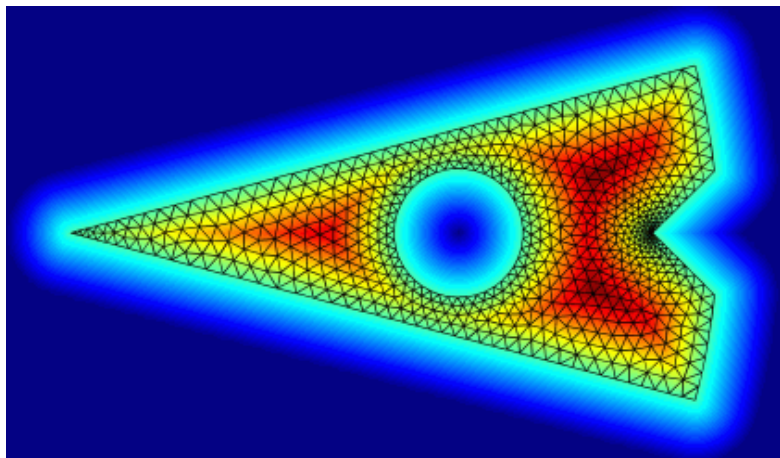
41: CVT: Centroidal Voronoi Tessellation

Voronoi diagram, step 65 **Delaunay triangulation, step 65**



https://people.sc.fsu.edu/~jburkardt/m_src/cvt_square_uniform_test/cvt_square_uniform.png

42: A CVT Mesh for the Holey Pie

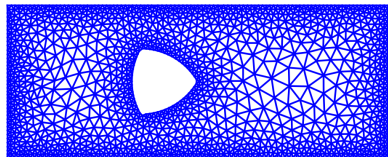


Is there time for a quick movie?

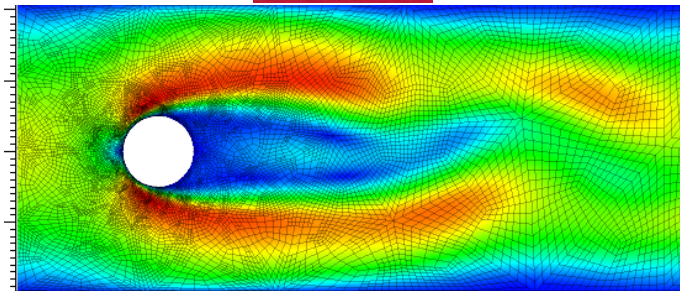
https://people.sc.fsu.edu/~jburkardt/presentations/cvt_movie_p08_cramped.mp4

xdg-open cvt_movie_p08_cramped.mp4

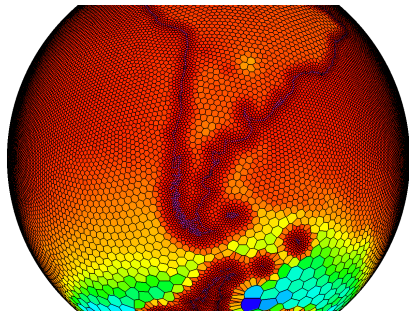
44: Meshes that Adapt to Flat or Curved Surfaces



45: 2D: A Moving Mesh for Fluid Flow

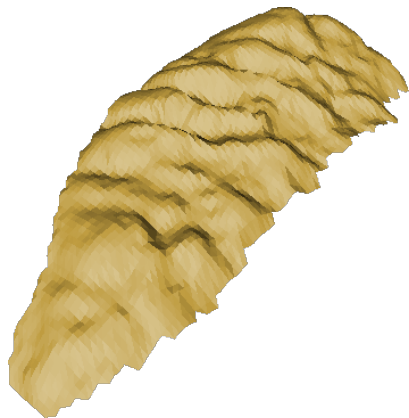


47: $2\frac{1}{2}$ D: Accurate Mesh of Coastline Interfaces



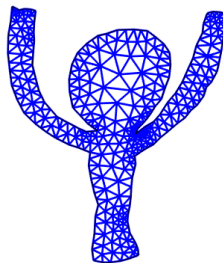
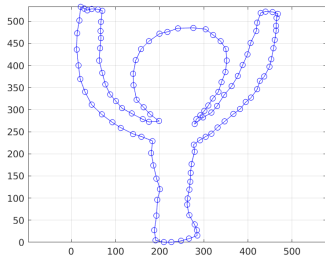
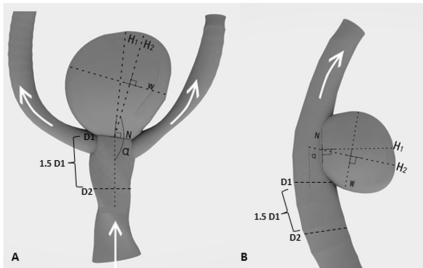
<https://www.linkedin.com/in/geoff-womeldorff-030112153/>

48: $2\frac{1}{2}$ D: Scan, Mesh and Classify Bones for Age-At-Death



<https://www.linkedin.com/in/detelina-stoyanova-05912876/>

49.5: When Will a Blood Vessel Burst?

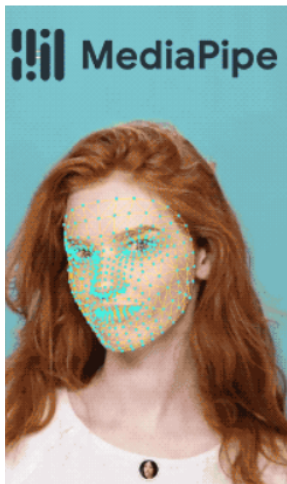


49.6: Computer Games Use Meshes



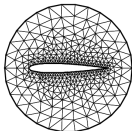
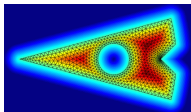
An example mesh editor for the Unity game engine.

49.7: Google MediaPipe

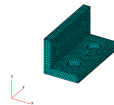


<https://google.github.io/mediapipe>

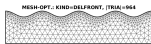
49.8: Meshing Programs



Gmsh



 MediaPipe

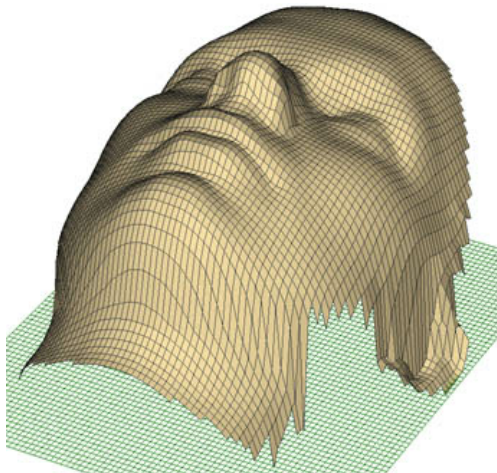


PyMesh



distmesh, freefem++, gmsh, matlab, mediapipe, mesh2d, meshlab, pymesh, triangle

50: A Flatbed Scanner Makes a Surface Mesh



<https://www.library.pitt.edu/3d-scanning-printing>

51: A Wrap-Around Scanner for Head-Protection Studies



https://morphlab.sc.fsu.edu/people/lab_members.html

Is there time for a another movie?

https://people.sc.fsu.edu/~jburkardt/presentations/head_scan_movie.mp4


xdg-open head_scan_movie.mp4

53: Results of a Wrap-Around Scan



https://people.sc.fsu.edu/~jburkardt/presentations/my_head.ply

54: Careers for Applied Mathematics Majors



CAREERS in applied mathematics

OPTIONS FOR STEM MAJORS

siam SOCIETY FOR INDUSTRIAL AND APPLIED MATHEMATICS

KAITLYN BRADY / DATA SCIENTIST

WHAT SHE DOES // No two days are ever the same for Kaitlyn. As a data scientist it is her responsibility to extract and communicate actionable insights from data. Her role centers on understanding her company's customers. Who are they? What are their preferences? Through knowledge of their customer she may better tailor their experience and in turn increase company performance. Recently she worked on building a personalized product recommendation engine from design to execution, including scoping the problem, building the algorithms, and writing the code.

NECESSARY JOB SKILLS // To be a data scientist you must be well rounded with statistical, programming, and communication skills. In addition to subject matter expertise. Some of these skills may be learned on the job, particularly the latter. Creative problem solving is critical. Each problem is different from the last and won't fit a textbook mold. A data scientist must identify and sometimes innovate solutions that aren't always obvious.

Mathematics is important in allowing Kaitlyn to provide concrete, data-supported evidence for the recommendations and answers she provides to business. Rather than making a subjective judgment, she uses statistics to formulate a solution that is based on reason and logic. Examples of concepts she has implemented so far include: time series analysis, logistic regression, and non-parametric measures for hypothesis testing.

PROS AND CONS OF HER JOB // One of the more rewarding aspects of Kaitlyn's job is when she knows that she delivered something new and empowered a business partner to advance their campaign or project—leveraging computer programming to bring a solution to production in an efficient manner. Kaitlyn's least favorite thing is day-to-day reporting.

CAREER PATH // Kaitlyn found her first full-time job as a data solutions engineer through her school career fair. She was responsible for a lot of ad-hoc analysis and reporting and realized that she wanted to do more statistical based work. That's when she moved to Staples as a statistical analyst where she became responsible for campaign analysis and experimental design. After some time, her responsibilities once again led into reporting and so she made the move over to a data science team where the work is more research oriented with longer term projects. Kaitlyn's career path continues to evolve as she learns more about herself every day.

WITH EACH NEW ROLE I PICK UP ADDITIONAL SKILLS AND PASSIONS AND PUSH MYSELF TOWARDS A MORE DEFINED CAREER.

SALARY // An approximate salary range is \$90,000 to \$200,000—depending on education, experience, and location.

CAREER EXPECTATIONS AND ADVICE // Internships and applied projects are great ways for students to gain real-world experience that will teach them new skills, help them learn what they do and do not like, and to pad out their resume. For those just starting their career, don't stress over finding the perfect job right out of the gate—you are still developing and learning and will have plenty of opportunities to move around.



DON'T STRESS OVER FINDING THE PERFECT JOB RIGHT OUT OF THE GATE.

AFFILIATION

Staples, Inc.

LOCATION

Frammingham, MA

DEPARTMENT

Staples Digital Solutions

TITLE

Data Scientist

EDUCATION

B.S. Mathematics and

Psychology 2011

Worcester State

University

M.S. Applied Statistics

2012, Worcester

Polytechnic Institute

CAREER STAGE

Early—6 years

post bachelors





BIG

JOBS GUIDE

Business, Industry, and Government Careers
for Mathematical Scientists, Statisticians,
and Operations Researchers



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My talk today involves a subject that spreads across several fields of study. Although I enjoy the mathematics that is involved, what I am doing is probably most comfortable as an example of scientific computing. Scientific computing, or computational science, has only recently been recognized as its own area, and now degree programs and separate departments are appearing in colleges across the country.

I'd like to say that if you enjoy mathematics, or computer science or any science, but especially enjoy doing these things when there is a computer involved, and an interesting real life problem to solve, then a program in computational science might be worth considering.

Although my first career choice (age 6) was "farmer", my first sensible choice was "something about mathematics", because I loved reading the Mathematical Games articles by Martin Gardner.

Starting in mathematics, my interest in writing, education, programming and research has led me to Scientific Computing, and it's probably too late now to make any more big changes.

Mathematics intrigued me because it showed that simple things like numbers and shapes could actually have mysterious properties.

In high school, I read a math book that described a proof that it was possible to cut a ball up into a few pieces that could be reassembled to make two balls of the same volume as the original one. (This is the Banach-Tarski paradox.)

And I read that equations like $y = f(x)$ could not only describe lines and parabolas and cubics - there was also a formula $y = f(x)$ that corresponded exactly to the profile of my own face.

I decided this was too nonsensical to believe, but I really wanted to hang out with people who thought things up like this!

<https://www.quantamagazine.org/how-a-mathematical-paradox-allows-infinite-cloning-20210826/>

SLIDE 7

After getting a mathematics degree, I was working at Iowa State University (half time research, half time running the computer lab) when I walked into a graduate student's office and saw a plot on his computer screen that just didn't make sense to me.

It was beautiful and it was mathematical. That doesn't happen often!

My friend, Lili Ju, now a professor at the University of South Carolina, explained to me that this was actually an example of a kind of mesh that organized itself, almost the way it would happen in nature.

I've got to know more about this! I told him, and I spent some time learning what he had done and how it could be used.

And I think that leads me into my story...

The Egyptians used 3-4-5 triangles of rope to resurvey the Nile banks after floods.

The Greeks named geo-metry and trigono-metry, and Eratostenes used this to measure the size of the Earth, the tilt of the Earth's axis, the distance to the sun.

Artists discovered that a complex object could be copied by viewing it through a wire mesh, and then filling in the boxes.

The French revolution invented the meter, and then had to measure a section of longitude in order to figure out what the meter was. ("The Measure of the Earth" by Larrie Ferreiro.)

Mathematicians didn't see any reason to divide smooth space up into triangles, (until much much later), but engineers and computational scientists realized the same lesson that artists had discovered: a complex shape may be easier to work with if a regular mesh is used to break it into many similar pieces.

SLIDE 11

It's pretty easy to see how computers can be taught to count, by turning decimal numbers into binary numbers, binary numbers into strings of 0's and 1's, and 0's and 1's into electronic switches.

But how do I explain the shape of Mickey Mouse's head? The area of lake Erie? The branching pattern of a human lung?

Let's take a shape that's not too simple, but not so complex, and "teach" the computer to see it.

Let's lower our expectations, and assume that the shapes we describe will be drawn using a sequence of straight lines. This means we're working with poly-gons (Greek for "many sides").

SLIDE 12

Using a polygon, we can still ask many interesting geometric questions, including

- perimeters,
- areas,
- centers of mass,
- whether a point is inside or outside a shape,
- the integral of some function over the triangle $\int_T f(x, y) dx dy$;
- the distance between a point and a shape
- can I get through a maze?
- how many objects can fit inside this shape?
- do these two shapes fit together?

Answering these questions is sometimes easy for us - but how do we teach the computer to do this?

If we have a shape outlined by straight lines, it is always possible to regard it as a collection of triangles.

My hand is an interesting shape (at least to me). Using a program like MATLAB, we can record points on my hand's outline so the computer can "see" what I see.

My hand is represented by a polygon. I don't know a lot about polygons, but I do know a lot about triangles. As it turns out, any polygon can be dissected into triangles, by "slicing off one ear at a time." And you can teach the computer to do this.

Thanks to the Greeks, we know lots of things about triangles, such as the area. There's a formula for the area of any triangle with vertices A , B , C . Using this, I can get the area of (the polygon representing) my hand.

It is possible to get a **negative area**. Indeed, if $A = (0,0)$, $B = (1,4)$, $C = (3,2)$, we get $\text{area}(A,B,C) = -5$. Interestingly enough, $\text{area}(A,C,B) = +5$.

The minus sign is telling us something very useful: the triangle (A,B,C) has its vertices listed in clockwise order, but (A,C,B) lists them in counterclockwise order, The sign of the area is a warning about the orientation of the triangle.

As long as we promise to list triangle vertices in counterclockwise order, we will have no problems with the area formula. But it turns out that this bit of knowledge can be used to determine other information.

Suppose I have a shape that I have turned into a polygonal outline, and then into a collection of triangles.

And now suppose I ask whether the point P is inside the shape? P is inside the shape (or at least the polygon) if it is inside a triangle. And it is inside triangle ABC exactly if all three subtriangles formed by P have positive area.

So that means we can solve the "point inside shape" geometry problem.

Many physical laws can be expressed in terms of integrals. Problems in heat conduction, fluid flow, elasticity, can be written this way. They can be solved if we can estimate integrals over the triangles of a mesh.

The finite element method rewrites a physical law in integral form, redraws the physical region as a mesh of triangles, estimates integrals over the triangles, and produces an approximate solution for the problem.

To approximate an integral over a triangle, there is an extensive family of quadrature rules that explain how to sample the function and weight the results.

https://people.sc.fsu.edu/~jburkardt/datasets/quadrature_rules_tri/quadrature_rules.tr

We measure temperature at a few places, but ask for its value anywhere.

To make a good estimate, we need to take the nearest data and somehow spread it to the query point.

If our data is on the vertices of triangles, then for any point P , we can find the triangle containing P , and use the triangle average of the vertex data. That is, the value at P is constructed by using the values at A , B , and C in the proportions of the triangles PBC , APC , and ABP .

Our estimates are most accurate if the triangles are regular shaped and relatively small.

Triangulating the hand completely covers the internal area, but it does so with triangles of many different sizes and shapes.

There might be reasons that we want a pattern of triangles that covers the region more evenly in shape and size.

mesh2d is a computer program for which the user only has to describe an outline of the region of interest, that is, a counterclockwise list of points.

We will start by asking for a simple mesh of a simple region, and then push the code little by little to harder tasks.

Describing the boundary of our region is easy.

mesh2d creates a simple triangular mesh.

If we add two points to the boundary, **mesh2d** takes the hint and includes more triangles in that area.

We can even specify a maximum triangle size so that **mesh2d** will fill up the region as we wish.

We can even specify that the triangle size changes in a way that suits us. Here, a related program called **distmesh** makes sure we have very small triangles near the inner corner of the region.

We can do similar operations on the hand data.

mesh2d creates a simple triangular mesh, with many internal vertices.

We can specify a maximum triangle size of 0.025 inches.

We can specify that triangles should be small near the edges, using a feature that **mesh2d** provides.

The “computer flower” I saw on Lili Ju’s computer screen is an example of a special mesh called a Centroidal Voronoi Tessellation (CVT), a favorite research topic of FSU professor Max Gunzburger.

In nature, for example, the tilapia form nests on a sandy river bottom, and somehow manage to make a mesh there.

To come up with a corresponding computer algorithm, you can imagine letting loose a swarm of bees into a small room, and assume every bee wants to avoid the other bees, and the walls, as much as possible. The resulting pattern is a CVT.

We often want meshes that are fine in some areas and coarse in others. That feature can be included in the CVT.

CVT’s are computed using iteration; that is, we make an initial guess for the mesh, and then repeatedly improve it. Here’s a short movie that suggests how this works.

Professor Max Gunzburger investigated the creation and use of these special meshes for regions, surfaces, and volumes.

FSU graduate student Lukas Bystricky studied the flow of fluids past obstacles. Behind the obstacle, the fluid whips up and down, and Lukas makes a mesh that follows the fluid action.

FSU postdoc Mauro Perego (now at Sandia lab) studied the slow flow of the gigantic ice sheet over Greenland. In order to get good results, he had to use detailed information about the coastline, about the height of the land surface below the ice, and about the average ice sheet velocity at each point.

FSU graduate student Geoff Womeldorff (now at Los Alamos lab) created meshes on the land and ocean, with very small elements where land and ocean overlap, in order to do climate studies.

Using this idea, FSU graduate student Detelina Stoyanova estimated the age of skeletons by scanning a particular bone, creating a mesh of triangles, which could then be compared against an online collection of such scans.

Undergraduates Marcelina Nagales and Alexa Pennavarria used the scanner to start a scientific scheme for classifying early North American arrowheads by style, region, and age.

Pitt Professor Catalin Trenchea is working on a project which is trying to give some mathematical insight into a deadly medical problem known as an aneurysm. When a blood vessel wall develops a weak spot, the high interior pressure can gradually push out a balloon-shaped distortion. At some point the stretched surface can break suddenly, releasing an uncontrolled flow of blood into the body or the brain.

This study is looking for ways of understanding the stresses on the surface wall, the different kinds of shapes that can develop, and the signs that might tell whether an aneurysm is simply a mild distortion, or a serious danger that may break soon.

As part of the study, sample diagrams of aneurysms must be outlined, and meshed, allowing a model of the internal blood flow and pressure to be developed.

FSU Professor Dennis Slice ran a geometric morphology lab. He has always had a 2D scanner, but now he has a 3D head scanner, for research on helmet design. FSU graduate student Alex Townsend sat me down in the barber's chair and promised me it wouldn't hurt.

A laser measures hundreds of thousands of points on the head.

A computer program can then organize these points into a triangular mesh representing the shape of the head.

You may remember that I mentioned at the beginning that mathematics promised me that an equation for the profile of my face "existed", although it offered no way of discovering it. Computational Science has produced a very reasonable result.

It's may be just an approximation, but now I can bet my head on it!

One place to get a realistic view of job opportunities for an applied mathematics major is the web site for SIAM (the Society for Industrial and Applied Mathematics). Their brochure on "Careers in Applied Mathematics" includes profiles of people in many careers, how they got there, what they do, and what they are earning. You need to start thinking about life after school, and this brochure is one way to get some ideas of the choices available to you.

Most job opportunities for mathematics majors are NOT in the university, but rather in business, industry, and government. These fields can be unfamiliar to anyone who has spent their life in school. SIAM publishes a friendly, information book, "The BIG Job Guide", which goes over the kind of jobs available, how to apply for them, what to expect if you get called in for an interview, what your working days will be like if you get hired, and the chances for promotion, salary, travel, and further training.